## UNIVERSITY OF SASKATCHEWAN **ELECTRICAL ENGINEERING 455.3**

Assignment Quiz 7 November 21, 2001

Instructor: B.L. Daku Time: 15 minutes Aids: None

Name:

Student Number:

1. When the input to an LTI system is

$$x[n] = \left(\frac{1}{3}\right)^n u[n] + 2^n u[-n-1],$$

the corresponding output is

$$y[n] = 5\left(\frac{1}{3}\right)^n u[n] - 5\left(\frac{2}{3}\right)^n u[n].$$

- (a) Find the system function H(z) of the system. Plot the pole(s) and zero(s) of H(z)and indicate the region of convergence.
- (b) Find the impulse response h[n] of the system.
- (c) Write a difference equation that is satisfied by the given input and output.

(d) Is the system stable? Is it causal?

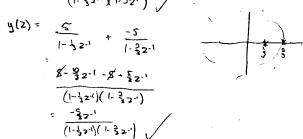
$$\chi(z) = \frac{1}{1 - \frac{1}{3} z^{-1}} + \frac{1}{1 - \frac{1}{3} z^{-1}} + \frac{1}{1 - \frac{1}{3} z^{-1}}$$

$$= \frac{x \cdot 2z^{-1}}{(1 - \frac{1}{3} z^{-1})(1 - 2z^{-1})}$$

$$= \frac{z}{2} z^{-1} + \frac{1}{1 - 2z^{-1}}$$

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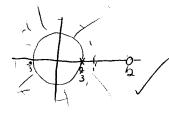


$$H(z) = \frac{-\sqrt{2}z^{-1}}{(1-\sqrt{2}z^{-1})(1-\sqrt{2}z^{-1})} \cdot (1-\sqrt{2}z^{-1})$$

$$H(z) = \frac{1-\sqrt{2}z^{-1}}{1-\frac{2}{3}z^{-1}} \cdot (1-\sqrt{2}z^{-1})$$

$$|z| > \frac{2}{3}.$$





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Name:

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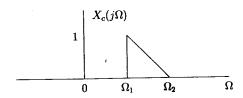
Student Number:

2)

Instructor: B.L. Daku

Time: 15 minutes

1. A complex-valued continuous-time signal,  $x_c(t)$ , has the Fourier transform shown in the following figure. The signal is sampled to produce the sequence  $x[n] = x_c(nT)$ .



- (a) Sketch the Fourier transform,  $X(e^{j\omega})$ , of the sequence x[n] for  $T = \pi/\Omega_2$ .
- (b) What is the lowest sampling frequency that can be used without incurring any aliasing distortion, i.e., so that  $x_c(t)$  can be recovered from x[n]. Show your work. Sketch  $X(e^{j\omega})$  using this sampling frequency.
- (c) Draw the block diagram of a system that can be used to recover  $x_c(t)$  from x[n]if the sampling rate is greater than or equal to the rate determined in part b). Assume that (complex) ideal filters are available.

